

Math 1720 Homework 6, due Friday Mar 2.  
Explain all answers and show all calculations.

7.4: 16, 19, 21, 25, 26  
Problems A, B.

Hint: note that in 7.4: 16, the data being described is the *rate* of oil consumption, not the quantity of oil consumed.

A. A function  $f(x)$  has exponential growth and a doubling time of  $T_2 = 0.4$ . Suppose  $f(2) = 16$ . Find the formula for  $f(x)$  and find  $f(0)$ .

B. A steamship is initially travelling along in a straight line, at a constant speed. At the stroke of midnight, it cuts its propellers. Its velocity function  $v(t)$  has exponential decay, where  $v(t)$  is the velocity in meters per second, at  $t$  seconds after midnight. Suppose that its velocity decreases by 2% every second (after cutting its propellers), and after 1 minute its velocity is 15 meters per second.

- (i) Find the ship's original velocity at midnight.
- (ii) Find the half-life of the velocity function, and use this to determine how long it will take the ship to slow to  $1/16$  of its midnight speed.
- (iii) Find the total distance travelled by the ship over the time interval from 11:59pm to 12:01am.