Projects in the Classroom

Neal Brand

Professor
Department of Mathematics
University of North Texas

April 7, 2018

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Tippe Tops and Calculus

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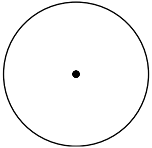

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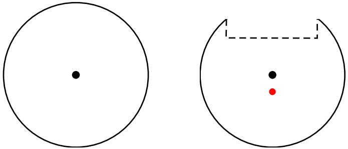

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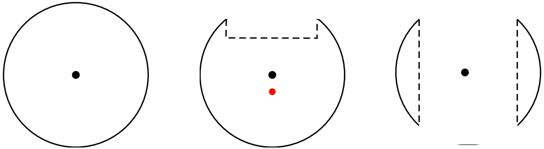

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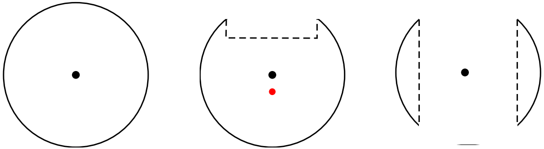

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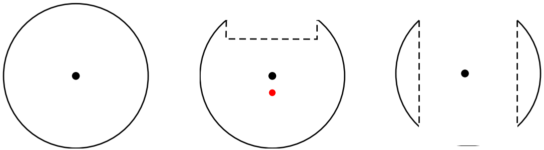

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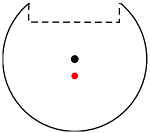

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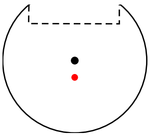

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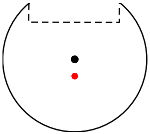

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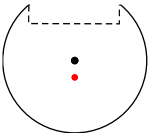

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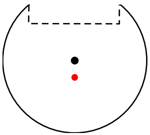

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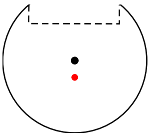

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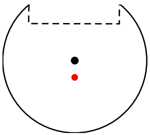

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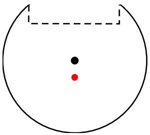

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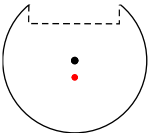

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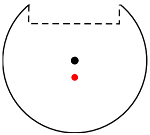

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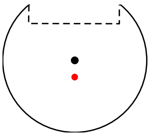

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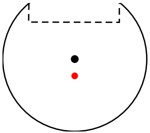

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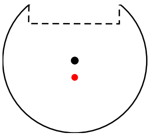

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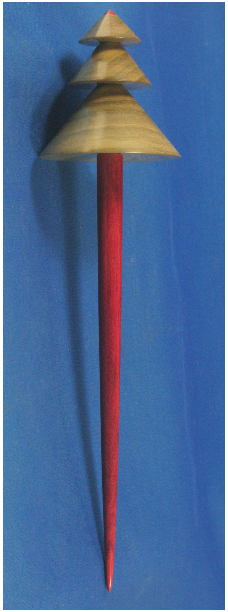

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Copies of these slides and the projects listed can be found at:
math.unt.edu/$\sim$brand